Q1 (5pts): Find a polynomial interpolation of degree 3 such that P(-1)=P(0)=1, P(1)=3 and P(2)=1 where

$$P(x) = a_0 x^3 + a_1 x^2 + a_2 x + a_3$$

Graph the data and the function on the same graph.

Hite: generate set of liner question and solve them to get the values of a₀, a₁,a₂, and a₃

Q2 (5pts): Perform a polynomial interpolation of degree 3 on the following data points:

$$x = [-2, 0, 1, 2] y = [-5, 1, 2, -1]$$

- a) Generate the Divided Difference Table
- b) Use (a) to produce the polynomial interpolation function.
- c) Graph the data and the function on the same graph.

Q3 (5pts): Perform a Lagrange interpolation on the following data points:

$$x = [-2, 0, 1, 2] y = [-5, 1, 2, -1]$$

- a) Find the value of the function at x = 0.5.
- b) Graph the data, value of the function at x = 0.5, and the function on the same graph.

Q4 (5pts): Evaluate the integral

$$\int_{1}^{2} \frac{1}{1+x} dx$$

Using one interval and Multiple Application. Compare the error of each method for one interval and how many integral is required to reduce the relative error to 0.01%

- a) Exact solution
- b) Trapezoid method
- c) Simpson's 1/3-Rule
- d) Simpson's 3/8-Rule
- e) Monte Carlo